

NAME: \_\_\_\_\_ PERIOD: \_\_\_\_\_ DATE: \_\_\_\_\_

LAB PARTNERS: \_\_\_\_\_ LAB #40

## ECCENTRICITY OF PLANETARY ORBITS

### INTRODUCTION

Our sun is not exactly in the center of the orbits of the planets, and therefore the planetary orbits are not circular. They are actually a curved figure known as an ellipse. The purpose of this laboratory is to learn more about the earth's orbit by experimenting with ellipses of different proportions. You will also study some characteristics of the sun that support the concept of an elliptical orbit.

### OBJECTIVES

During this laboratory investigation you will:

1. Draw ellipses of different proportions.
2. Calculate eccentricity from ellipse measurements.
3. Compare the eccentricity of the planets in our solar system.
4. Relate the changes in the sun's apparent diameter to the earth's elliptical orbit.

### MATERIALS

Pencil  
Two thumbtacks  
25 cm strong thread  
Cardboard (9 x 11 inches)  
Graph paper

APPROXIMATE TIME 1-2 Periods

## PART 1

### PROCEDURE

1. Form a loop by tying the ends of a piece of thread 25 centimeters long. When the loop is held taut, it should be 11 centimeters long.
2. On the sheet containing the ellipse points, set the two thumbtacks into points A and B. Place the loop over the thumbtacks. Insert the sharp point of the pencil inside the loop. While keeping the loop taut around both thumbtacks, draw a curve around the two centers.
3. Repeat the same procedure using points C and D for the next ellipse. Then use points E and F to make another ellipse.
4. In an ellipse, each of the two central points is called a focus (they are both known as foci). Label the sets of point's foci.
5. The eccentricity (or amount of flattening) is determined by the ratio of the distance between the foci and the length of the major axis. The formula is in your earth science reference tables. Using the formula, calculate the eccentricity of each of the three ellipses that you drew. Record your answers in the spaces below.

Ellipse AB \_\_\_\_\_

Ellipse CD \_\_\_\_\_

Ellipse EF \_\_\_\_\_

## CALCULATION SHEET FOR ELLIPSES

### ELLIPSE AB

Distance between foci \_\_\_\_\_ cm

Major axis length \_\_\_\_\_ cm

Answer \_\_\_\_\_

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### ELLIPSE CD

Distance between foci \_\_\_\_\_ cm

Major axis length \_\_\_\_\_ cm

Answer \_\_\_\_\_

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### ELLIPSE EF

Distance between foci \_\_\_\_\_ cm

Major axis length \_\_\_\_\_ cm

Answer \_\_\_\_\_

EXERCISES ON THE BINARY SYSTEM

EXERCISE 1

1. Let  $x$  be a number in the interval  $(0, 1)$ . Write  $x$  in binary form. Let  $n$  be a positive integer. Let  $x_n$  be the number obtained by truncating the binary expansion of  $x$  after  $n$  digits. Show that  $|x - x_n| < 2^{-n}$ .

EXERCISE 2

1. Let  $x$  be a number in the interval  $(0, 1)$ . Write  $x$  in binary form. Let  $n$  be a positive integer. Let  $x_n$  be the number obtained by truncating the binary expansion of  $x$  after  $n$  digits. Show that  $|x - x_n| < 2^{-n}$ .

$\oplus F$

$\oplus D$

EXERCISE 3

1. Let  $x$  be a number in the interval  $(0, 1)$ . Write  $x$  in binary form. Let  $n$  be a positive integer. Let  $x_n$  be the number obtained by truncating the binary expansion of  $x$  after  $n$  digits. Show that  $|x - x_n| < 2^{-n}$ .

$\oplus B$

$\oplus A$

PART 1

EXERCISE 4

1. Let  $x$  be a number in the interval  $(0, 1)$ . Write  $x$  in binary form. Let  $n$  be a positive integer. Let  $x_n$  be the number obtained by truncating the binary expansion of  $x$  after  $n$  digits. Show that  $|x - x_n| < 2^{-n}$ .

$\oplus C$

$\oplus E$

2. Let  $x$  be a number in the interval  $(0, 1)$ . Write  $x$  in binary form. Let  $n$  be a positive integer. Let  $x_n$  be the number obtained by truncating the binary expansion of  $x$  after  $n$  digits. Show that  $|x - x_n| < 2^{-n}$ .

Exercise A1

Exercise C1

Exercise E1

**LABORATORY QUESTIONS**

1. As the distance between the foci increases, how does the shape of the ellipse change?  
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2. As the distance between the foci increases, how does the eccentricity of the ellipses change?  
\_\_\_\_\_
3. The major axis of the earth's orbit is 186,000,000 miles in length. The distance between the sun and the second focus is 3,000,000 miles. What is the eccentricity of the earth's orbit?  
SHOW ALL WORK.

4. Which of the three ellipses that you drew do you think most closely represents the earth's orbit.

Why? \_\_\_\_\_

\_\_\_\_\_

**PART 2**

For the following three questions, use the chart below which gives information on the eccentricity of the planets in our solar system.

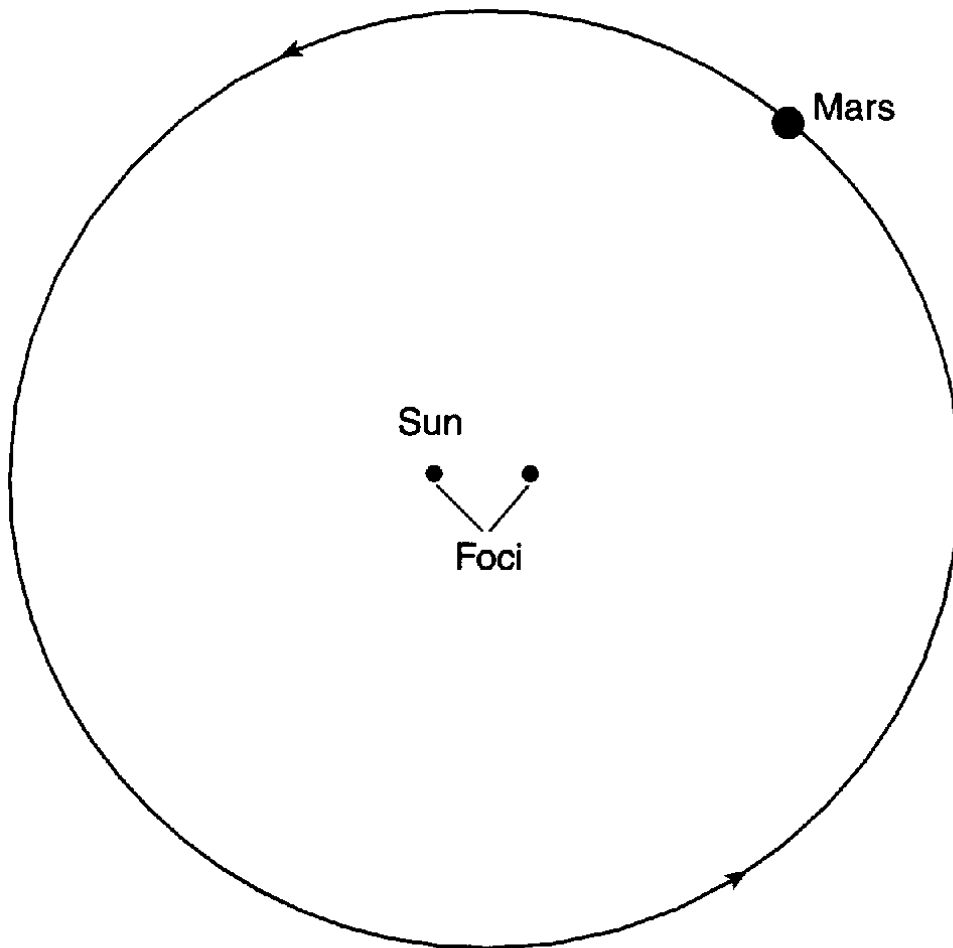
<b>PLANET</b>	<b>MAJOR AXIS (MILES)</b>	<b>ECCENTRICITY</b>
Mercury	72,000,000	0.206
Venus	134,000,000	0.007
Mars	284,000,000	0.093
Jupiter	966,000,000	0.048
Saturn	1,772,000,000	0.056
Uranus	3,560,000,000	0.047
Neptune	5,580,000,000	0.008

1. Which planets have almost circular orbits?  
\_\_\_\_\_
2. Which planets have the most eccentric orbits?  
\_\_\_\_\_
3. How does the eccentricity of the earth compare with the eccentricity of the other planets?  
\_\_\_\_\_

**PART 3**  
**ORBITAL VARIATIONS**

**PROCEDURE:**

1. **Draw and label** the major axis for Mars orbit.
2. Place a **point** on Mars orbit and label it number **1** to represent the position where Mars orbital velocity would be fastest.
3. Place a **point** on Mars orbit and label it **2** to represent the position where Mar's orbital velocity would be slowest.



(Not drawn to scale)

**LABORATORY QUESTIONS**

1. Calculate the eccentricity of Mar's orbit based on the image above. (Show all work)

Distance between foci \_\_\_\_\_ cm

Major axis length \_\_\_\_\_ cm

Answer \_\_\_\_\_

2. Explain why you chose the position on Mars orbit where you drew point 1.

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3. At which numbered position would the force of gravity between the sun and Mars be the greatest? Explain why you chose that point?

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4. What two factors affect the force of gravity and the orbital velocity of Mars?

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5. If the mass of the sun were tripled what would happen to the gravitational force on the planet Mars?

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6. Chiron is a planetoid located in the outer solar system. It has an eccentricity of 0.379. Based on the eccentricity you calculated for the planet Mars, compare the **shape** of Chiron's orbit to that of Mars.

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7. Describe the true shape of Mars orbit.

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